

## EXERCISE ON IRF'S, GCP, SVAR'S

- (1) Here are two first-order, four-variable VARs. In each case, is there a way to order the variables so that they show a Granger causal ordering? What is the implied ordering (e.g.  $\{a, b\} \rightarrow d \rightarrow c$ )?

$$y_t = \begin{bmatrix} .1 & 0 & .3 & 0 \\ 0 & .9 & 0 & -.6 \\ .6 & 0 & -.3 & 0 \\ 0 & .1 & 0 & .1 \end{bmatrix} y_{t-1} + \varepsilon_t$$

$$y_t = \begin{bmatrix} 1 & 0 & .2 & .2 \\ 1 & 1 & 1 & 1 \\ 1 & 0 & .2 & .3 \\ -.6 & 0 & .8 & -.1 \end{bmatrix} y_{t-1} + \varepsilon_t$$

- (2) For one of the systems in question 1 that does display a Granger ordering (and at least one does), calculate the first three matrices of impulse response coefficients, assuming a diagonal covariance matrix of shocks so that no orthogonalization is needed. [You will want to use R or Matlab or the like for this calculation. On an exam, a question like this would probably stick to two by two matrices.] This problem should verify an important point not emphasized in the lecture: Block triangular structure in the AR coefficient matrices  $B(L)$  implies block triangular structure in  $B^{-1}(L)$ .
- (3) In a two-dimensional structural VAR we have three choices of identifying assumption, any one of which we think is plausible. The model has the usual form  $A(L)y = \varepsilon$  and we assume  $A_0^{-1}\varepsilon$  is the innovation. One possible identifying assumptions  $a_{210} = 0$  (i.e., the  $A_0$  matrix is upper triangular, so that  $y_2$  responds to shock 1 only with a 1-period delay). A second is instead  $a_{210} = a_{211} = 0$ , i.e. that it responds only with a 2-period delay. and a third is  $a_{210} = a_{211} = a_{120} = a_{121} = 0$ . One of these is much easier to handle than the others. Why? Explain how you could go about estimating the coefficients in  $A(L)$  in each case.

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