## **Preliminary Course Outline and Reading List**

This outline lays out the topics that we should try to cover in this course. Probably we can't cover them all. Parts of the outline are more detailed, with specific references, because they correspond to material from previous versions of this course. The less detailed parts of the outline will be filled in. If viewed online with Acrobat Reader, there should be clickable links in the text.

Kallenberg (2002) is an advanced, thorough, account of probability and stochastic process theory. It assumes solid grounding in real analysis and measure theory. It is listed here only as a reference, for students whose mathematical background is strong and may want to pursue topics in this course at a more advanced or rigorous level. The Hamilton (1994) book covers many of the models used in time series econometrics and that we will deal with in this class. Hamilton proceeds more slowly through the material than we will in this class and he gives more emphasis to non-Bayesian asymptotic theory of inference than we will (and less to Bayesian inference). The Bauwens, Lubrano, and Richard (1999) book is closer in approach to this course than is Hamilton's but because of its variations in mathematical level and choice of topics only parts of it are assigned reading.

This course will primarily discuss inference from a Bayesian perspective. Since this perspective is sometimes given scant attention in the Princeton first-year econometrics sequence, we will introduce and review Bayesian inference ideas as we encounter them. The 2004 version of ECO517 gave a systematic introduction to Bayesian inference; if you have had little or no previous exposure to those ideas, you might find it useful to look at course materials from that version of the course, which are available online, and/or any of the books Schervish (1995), Robert (1994), Berger (1985), Geweke (2006), Lancaster (2004) and Gelman, Carlin, Stern, and Rubin (1995). They have somewhat different choices of topics and assume varying levels of mathematical background, with Schervish the most demanding and Lancaster or Gelman et al the least, in this respect. Geweke and Lancaster are both oriented toward econometrics, while the others are oriented toward statistics. A reference for Monte Carlo computational methods for sampling from posterior densities is Robert and Casella (2004).

There will be exercises that assume you are able to use a programming language like S, R, Matlab, Scilab, Octave, or possibly Mathematica, to carry out matrix algebra calculations and to run iterative algorithms. R and Octave are free, open-source software. R is almost identical, as a language, to S, but has a limited graphical interface (GUI). (Its ability to produce graphs is not limited. It just has limited ability to produce menus and let you initiate actions with mouse clicks.) Octave is similarly very close as a language to Matlab, while having a more limited GUI. S and Matlab and R are available on the departmental computer cluster and on the university's network servers hats.princeton.edu and arizona.princeton.edu. If you use, or want to try, R, good references are Venables and Ripley (2001) and Venables and Ripley (2002).

<sup>© 2006</sup> by Christopher A. Sims. This document may be reproduced for educational and research purposes, so long as the copies contain this notice and are retained for personal use or distributed free.

None of the books are required for purchase, but any of those listed that fit your mathematical and statistical background would be good investments, both for this course and later reference.

### 1. Inference: Bayesian basics

- (a) Decision theory
- (b) Complete class theorems
- (c) Likelihood principle
- (d) Bayesian scientific reporting

### 2. Stochastic processes

- (a) Probability as  $(S, \mathcal{F}, \mu)$  triple.
- (b) Conditional expectation, conditional probability
- (c) Discrete and continuous time processes
- (d) i.i.d discrete time processes
- (e) First finite-parameter family of processes: Discrete time Gaussian MA processes; their likelihood; uniqueness.

#### 3. General Gaussian stationary processes

- (a) Autocovariance function
- (b) Spectral density
- (c) Ergodicity
- (d) Mixing conditions
- (e) One-sided inversion of convolution operators.
- (f) Innovations, fundamental MA representation.
- (g) Linearly deterministic and linearly regular processes, the Wold decomposition
- (h) Seasonality
- (i) Time aggregation

## 4. The ARMA family of processes

- (a) AR processes
- (b) MA processes
- (c) Density in the Gaussian stationary class

## 5. Inference for ARMA models: The Kalman filter.

- (a) Priors and posteriors for the standard normal linear model
- (b) The Kalman filter
- (c) Initialization
- (d) AR coefficients as states

- (e) Lagged innovations in MA models as states
- (f) The Kalman filter as a component of likelihood-based inference
- (g) Smoothing vs. filtering
- 6. Importance Sampling, Metropolis-Hastings MCMC
  - (a) Importance sampling and its pitfalls
  - (b) Metropolis Markov Chains and their pitfalls
  - (c) Metropolis-Hastings
  - (d) "Gibbs" Sampling
  - (e) Assessing convergence
  - (f) Computing marginal data density
  - (g) Particle filtering
  - (h) Application to ARMA models nonlinear in parameters: Linearized DSGE models.

(Hamilton, 1994, section 12.3)

Gelman, Carlin, Stern, and Rubin (1995), Chapter 11

Notes: "Proof of Fixed Point Property for Metropolis Algorithm"

- 7. ARMA models nonlinear in parameters: Linearized DSGE models.
  - (a) The Smets and Wouters project

Smets and Wouters (2003)

- 8. High-order and multivariate AR models
  - (a) Review of multivariate linear stochastic difference equations
    - i. Roots to qualitatively characterize models
    - ii. Impulse response functions
      - A. Impulse responses vs. ACF's as data summaries
  - (b) Exogeneity, Granger causality, Wold and Granger causal orderings
  - (c) Structural VAR's and identification
    - i. Delay restrictions
    - ii. Long run restrictions
    - iii. Restrictions on impulse responses
  - (d) Stochastic volatility and GARCH
  - (e) Factor models

(Hamilton, 1994, Chapters 10.1-10.3)

- 9. Hidden Markov chain and non-recurrent break models
  - (a) Structural breaks
  - (b) Regime shifts
  - (c) Approximation to parameter change and stochastic volatility models

Hamilton (1994), Chapter 22 Chib (1996)

- 10. Modeling initial conditions and "trend"
  - (a) High-order AR + conditioning on initial conditions + flat prior ⇒ belief in likely historical uniqueness of sample start date
  - (b) Unit roots
  - (c) Cointegration
  - (d) Fractional integration
  - (e) Realistic modeling of uncertainty about the long run vs. "removing trend".

(Sims, 2000) (Sims, 1989) (Sims, revised 1996) (Hamilton, 1994, section 19.1) (Sims and Uhlig, 1991)

11. Dummy-observation priors for VAR's

(Sims and Zha, 1998)

Notes: Dummy observation priors

- 12. Formulating, using, testing restrictions or priors on VAR's
  - (a) Recursiveness restrictions
    - i. Exogeneity and likelihood structure (Bauwens, Lubrano, and Richard, 1999, sections 2.6, 5.2.1-2)
  - (b) Priors and restrictions for structural VAR's
    - i. Litterman/Leeper/Sims/Zha
    - ii. Long run restrictions
    - iii. Priors on impulse responses
    - iv. Reduced form vs. structural parameters as space for prior
    - v. Error bands for impulse responses

(Hamilton, 1994, Chapters 11, and 9, section 12.2)

Notes: "Granger Causality" (There is some redundancy between these notes and the set below.)

Notes: Likelihood for VAR systems Blanchard and Quah (1989) Leeper, Sims, and Zha (1996) Sims and Zha (1998) Sims and Zha (1999) DelNegro, Schorfheide, Smets, and Wouters (2006)

#### 13. More models

- (a) Dynamic factor models
- (b) Stochastic volatility
- 14. Inference: Asymptotic theory
  - (a) Central limit theorems and functional central limit theorems
  - (b) Bayesian and sampling theory asymptotics: differences and connections
  - (c) Asymptotics do not free us from assumptions
  - (d) Asymptotics for nonstationary models

# References

- BAUWENS, L., M. LUBRANO, AND J.-F. RICHARD (1999): *Bayesian Inference in Dynamic Econometric Models*. Oxford University Press.
- BERGER, J. O. (1985): *Statistical Decision Theory and Bayesian Analysis*, Springer Series in Statistics. Springer, 2nd edn.
- BLANCHARD, O., AND D. QUAH (1989): "The Dynamic Effects of Aggregate Demand and Supply Disturbances," *American Economic Review*, 79, 655–73.
- CHIB, S. (1996): "Calculating Posterior Distributions and Modal Estimates in Markov Mixture Models," *Journal of Econometrics*, 75, 79–98.
- DELNEGRO, M., F. SCHORFHEIDE, F. SMETS, AND R. WOUTERS (2006): "On the Fit of New-Keynesian Models," Discussion paper, Federal Reserve Bank of Atlanta.
- GELMAN, A., J. B. CARLIN, H. S. STERN, AND D. B. RUBIN (1995): *Bayesian Data Analysis*. Chapman and Hall, London, 1st edn.
- GEWEKE, J. (2006): *Contemporary Bayesian Econometrics and Statistics*, Wiley Series in Probability and Statistics. Wiley.
- HAMILTON, J. D. (1994): Time Series Analysis. Princeton University Press, Princeton, NJ.

- KALLENBERG, O. (2002): *Foundations of Modern Probability*, Probability and its Applications. Springer, New York, Berlin, Heidelberg, second edn.
- LANCASTER, T. (2004): An Introduction to Modern Bayesian Econometrics. Blackwell.
- LEEPER, E. M., C. A. SIMS, AND T. ZHA (1996): "What Does Monetary Policy Do?," *Brookings Papers on Economic Activity*, (2), 1–78.
- ROBERT, C. (1994): *The Bayesian Choice*, Springer Texts in Statistics. Springer-Verlag, New York.
- ROBERT, C. R., AND G. CASELLA (2004): *Monte Carlo Statistical Methods*, Springer Texts in Statistics. Springer, 2nd edn.
- SCHERVISH, M. J. (1995): *Theory of Statistics*, Springer Series in Statistics. Springer, New York.
- SIMS, C. A. (1989): "Modeling Trends," in *Proceedings*, American Statistical Association Annual Meetings, http://sims.princeton.edu/yftp/trends/asa889.pdf.
- ——— (2000): "Using a Likelihood Perspective to Sharpen Econometric Discourse: Three Examples," *Journal of Econometrics*, 95(2), 443–462, http://www.princeton.edu/~sims/.
- ——— (revised 1996): "Inference for Multivariate Time Series with Trend," Discussion paper, presented at the 1992 American Statistical Association Meetings, http://sims.princeton.edu/yftp/trends/ASAPAPER.pdf.
- SIMS, C. A., AND H. D. UHLIG (1991): "Understanding Unit Rooters: A Helicopter Tour," *Econometrica*, 59(6), 1591–1599.
- SIMS, C. A., AND T. ZHA (1998): "Bayesian Methods for Dynamic Multivariate Models," *International Economic Review*.
- ——— (1999): "Error Bands for Impulse Responses," *Econometrica*, 67(5), 1113–1156.
- SMETS, F., AND R. WOUTERS (2003): "An Estimated Dynamic Stochastic General Equilibrium Model of the Euro Area," *Journal of the European Economic Association*, 1, 1123–1175.
- VENABLES, W. N., AND B. D. RIPLEY (2001): *S Programming*, Statistics and Computing. Springer.
- ——— (2002): *Modern Applied Statistics with S*, Statistics and Computing. Springer.