

## FINAL EXAM FOR FIRST HALF

*This exam is due at noon Friday, October 27. I prefer that the submissions be in electronic form, by email. If your answers are handwritten, stick them under my office door, or give them to me if I am there, and send me an email saying you have done so.*

*You are not to discuss the exam with anyone else between noon Thursday and noon Friday, when it is due.*

- (1) Consider a farmer who grows wheat. He uses some of it to make bread for himself, and he sells the rest in a competitive market at price  $P$  for apples, which he eats.  $\bar{W}$  is the amount of wheat he has grown,  $W$  is the amount of wheat he eats, and  $A$  is the amount of apples he eats. His utility is

$$U(W, A) = \sqrt{W} + \sqrt{A}$$

and his budget constraint is of course

$$A = P \cdot (\bar{W} - W).$$

He knows  $\bar{W}$  but is uncertain about  $P$ , and has an initial distribution for it with density

$$g(P) = Pe^{-P},$$

i.e. a Gamma(2) pdf. He has a cost of information of  $\theta$  units of utility per nat and wishes to choose  $W$  and his information to maximize expected utility minus information costs.

- (a) Write down the objective function and constraints for this problem.
- (b) Display the first order conditions for an optimum for the problem.
- (c) Find the pdf of  $W$  in the case when the cost of information  $\theta$  is zero. What is its support?
- (d) See if you can prove that the distribution of  $W$  cannot have the full support of the  $\theta = 0$  solution when  $\theta > 0$ . [Note that, unless you decide you want to prove it's discretely distributed, this argument should not require invoking properties of analytic functions. You will get some credit for describing a reasonable attempt at a proof, even if you can't fully complete it.]

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- (2) In the Davig and Leeper long run Taylor principle paper, they work out a condition on the inflation coefficients  $\alpha_1$  and  $\alpha_2$  and the transition probabilities that they call the long run Taylor principle. But at the start of the theorem they rule out  $\alpha_i < p_{ii}$  for either regime. They say that this is to “restrict the  $\alpha$ 's to the space containing the economically interesting portion of the hyperbola, in which monetary policy seeks to stabilize, rather than destabilize, the economy”. Can there in fact be stable solutions when  $\alpha_i < p_{ii}$  for some  $i$ ? If so, what is unreasonable about them? What do Davig and Leeper mean by saying these cases imply the monetary authority is trying to destabilize the economy?